

**Answers to Problems from section 2.8:**

4. and 7. Graphs omitted here. To be discussed in Monday Lecture, July 6th.

32.  $f$  is not differentiable at  $x = 0$ , because there is a discontinuity there, and at  $x = 3$ , because the graph has a vertical tangent there.

37.  $a = f$ ,  $b = f'$ ,  $c = f''$ . We can see this because where  $a$  has a horizontal tangent,  $b = 0$ , and where  $b$  has a horizontal tangent,  $c = 0$ . We can immediately see that  $c$  can be neither  $f$  nor  $f'$ , since at the points where  $c$  has a horizontal tangent, neither  $a$  nor  $b$  is equal to 0.

**Answers to Problems from section 2.9:**

2. (a)  $f'(x) > 0$  and  $f$  is increasing on  $(0,1)$  and  $(3,5)$ .  $f'(x) < 0$  and  $f$  is decreasing on  $(1,3)$  and  $(5,6)$ .

(b)  $f$  has local maxima at  $x = 1$  and  $x = 5$ , and it has a local minimum at  $x = 3$ .

8. (a) If the position function is increasing, then the particle is moving toward the right. This occurs on  $t$ -intervals  $(0,2)$  and  $(4,6)$ . If the function is decreasing, then the particle is moving toward the left – that is, on  $(2,4)$ .

(b) The acceleration is the second derivative and is positive where the curve is concave upward. This occurs on  $(3,6)$ . The acceleration is negative where the curve is concave downward – that is, on  $(0,3)$ .

21. (a) Since  $e^{-x^2}$  is positive for all  $x$ ,  $f'(x) = xe^{-x^2}$  is positive where  $x > 0$  and negative where  $x < 0$ . Thus,  $f$  is increasing on  $(0, \infty)$  and decreasing on  $(-\infty, 0)$ .

(b) Since  $f$  changes from decreasing to increasing at  $x = 0$ ,  $f$  has a minimum value there.

23. (a)  $f$  is increasing on  $\left(-\infty, -\sqrt{\frac{1}{3}}\right)$  and on  $\left(\sqrt{\frac{1}{3}}, \infty\right)$ .  $f$  is decreasing

on  $\left(-\sqrt{\frac{1}{3}}, \sqrt{\frac{1}{3}}\right)$ .

25.  $b$  is the antiderivative of  $f$ . For small  $x$ ,  $f$  is negative, so the graph of its antiderivative must be decreasing. But both  $a$  and  $c$  are increasing for small  $x$ , so only  $b$  can be  $f$ 's antiderivative. Also  $f$  is positive where  $b$  is increasing, which supports our conclusion.

**Answers to Problems from section 3.1:**

17. 0.

19.  $\frac{3}{2}\sqrt{x} + \frac{2}{\sqrt{x}} - \frac{3}{2x\sqrt{x}}$

22.  $ae^v - \frac{b}{v^2} - \frac{2c}{v^3}$

23.  $-\frac{10A}{y^{11}} + Be^y$

24.  $\frac{2}{3\sqrt[3]{t}} + 3\sqrt{t}$

25. Tangent Line:  $y = 2x + 2$ . Normal Line:  $y = -\frac{1}{2}x + 2$ .

38.  $G'''(r) = \frac{1}{4}r^{-3/2} - \frac{2}{9}r^{-5/3}$ .

47.  $m = y' = 18x^2 + 5$ , but  $x^2 \geq 0$  for all  $x$ , so  $m \geq 5$  for all  $x$ .

**Answers to Problems from section 3.2:**

5.  $\frac{e^x(x-2)}{x^3}$ .

9.  $5 + 14y^{-2} + 9y^{-4}$ .

10.  $3 + 3e^t - \frac{3}{2}\sqrt{t} - \sqrt{t}e^t - e^t/(2\sqrt{t})$ .

15.  $2v - v^{-1/2}$ .

$$16. \frac{5}{2} w^{3/2} + \frac{1}{2} cw^{1/2}e^w(2w + 3).$$

$$20. \frac{ad - bc}{(cx + d)^2}.$$

$$21. \text{Tangent Line: } y = 2x. \text{ Normal Line: } y = -\frac{1}{2}x.$$

$$30. g^{(n)}(x) = \frac{(x - n)(-1)^n}{e^x}$$

$$45. \text{ (a) } (fgh)' = [(fg)h]' = (fg)'h + (fg)h' = (f'g + fg')h + fgh' = f'gh + fg'h + fgh'$$

$$\text{ (b) Putting } f = g = h \text{ in part (a), we have } \frac{d}{dx}[f(x)]^3 = (fff)' = f'ff + ff'f + fff' = 3fff' = 3[f(x)]^2 f'(x).$$

$$\text{ (c) } \frac{d}{dx}(e^{3x}) = \frac{d}{dx}(e^x)^3 = 3(e^x)^2 e^x = 3e^{2x} e^x = 3e^{3x}.$$

**Answers to Problems from section 3.3:**

$$8. \text{ (a) Maximum height is 100 ft.}$$

$$27. 16 \text{ ft/s and } -16 \text{ ft/s.}$$

**Answers to Problems from section 3.4:**

$$5. \sec \theta (\sec^2 \theta + \tan^2 \theta) = \sec \theta (1 + 2 \tan^2 \theta) = \sec \theta (2 \sec^2 \theta - 1)$$

$$8. \frac{x \cos x}{(x + \cos x)^2}$$

$$13. -\csc x \cot x$$

$$14. \sec x \tan x$$

$$15. -\csc^2 x$$

$$18. y = x + 1.$$

31. (a)  $a(t) = -8 \sin t$

(b) The mass at time  $t = \frac{2\pi}{3}$  has position  $4\sqrt{3}$ , velocity  $-4$  and acceleration  $-4\sqrt{3}$ . It is moving to the left and it is speeding up.

36.  $-35 \sin x - x \cos x$ .

**Answers to Problems from section 3.5:**

10.  $\frac{\sec^2 t}{3\sqrt[3]{(1 + \tan t)^2}}$

12.  $-3 \sin x \cos^2 x$

19.  $e^{x \cos x} (\cos x - x \sin x)$

21.  $\frac{1}{(z-1)^{1/2}(z+1)^{3/2}}$

31.  $\cos(\tan \sqrt{\sin x}) \left(\sec^2 \sqrt{\sin x}\right) \left(\frac{1}{2\sqrt{\sin x}}\right) (\cos x)$

32.  $\frac{1}{2} \left(x + \sqrt{x + \sqrt{x}}\right)^{-1/2} \left[1 + \frac{1}{2} (x + \sqrt{x})^{-1/2} \left(1 + \frac{1}{2} x^{-1/2}\right)\right]$

34.  $e^{e^x} \cdot e^x (1 + e^x)$

36.  $y = x$ .

47.  $-17.4$

70.  $y = \frac{1}{2}x + \frac{1}{2}$

71.  $y = -\frac{2}{e}x + 2$