

# The Six Major Puzzles in International Macroeconomics: Is There a Common Cause?

Maurice Obstfeld and Kenneth Rogoff

International Finance

# Six major puzzles in International Macro

- 1 Home bias in trade
- 2 Feldstein-Horoika puzzle (small OECD current account balances relative to savings and investment)
- 3 Home bias in Portfolio
- 4 Low-consumption-correlations puzzle
- 5 Purchasing-power-parity puzzle (weak relationship between exchange rates and national price levels)
- 6 Exchange-rate-disconnect puzzle (weak relationship between exchange rates and virtually any macroeconomic aggregates)

# Findings

- Many of the puzzles can be resolved (to varying degrees) by incorporating significant (but plausible) trade costs
- Trade costs include transport costs, tariffs, nontariff barriers, and possibly other broader impediments to trade
- The authors' simple model with transport costs seems to be particularly successful in resolving real-side quantity puzzles, but would need a richer framework with imperfect competition and wage/price rigidities to address the pricing puzzles

# Puzzle 1: home bias in trade

- Trade among Canadian provinces was twenty times greater than trade between Canadian provinces and US states, controlling for distance, partner size, etc. (McCallum 1995)
- Falls to 12 after NAFTA (Helliwell 1998)
- Similar exercise extended to OECD countries can lower bias to 2.5 (Wei 1998), while Evans (1999) finds values intermediate between Wei's and Helliwell's

# Home bias in trade - a model

Consider a simple two country, two good, endowment economy.  
Utility maximization for home and foreign agents is given by

$$\begin{aligned} \max \quad & C \equiv \left( C_H^{(\theta-1)/\theta} + C_F^{(\theta-1)/\theta} \right)^{\theta/(\theta-1)} \\ \text{s.t.} \quad & P_H C_H + P_F C_F \leq P_H Y_H \end{aligned}$$

and

$$\begin{aligned} \max \quad & \left( C_H^{*(\theta-1)/\theta} + C_F^{*(\theta-1)/\theta} \right)^{\theta/(\theta-1)} \\ \text{s.t.} \quad & P_H^* C_H^* + P_F^* C_F^* \leq P_F Y_F \quad . \end{aligned}$$

# Home bias in trade - no arbitrage condition

Arbitrage implies

$$P_F = P_F^*/(1 - \tau)$$

$$P_H = (1 - \tau)P_H^*$$

where  $\tau$  is iceberg transportation costs. Then

$$p^* = p(1 - \tau)^2 \tag{1}$$

where  $p = \frac{P_F}{P_H}$  and  $p^* = \frac{P_F^*}{P_H^*}$ .

# Home bias in trade - first order conditions

FOCs are given by

$$\frac{C_H^{-1/\theta}}{C_F^{-1/\theta}} = \frac{P_H}{P_F}, \quad \frac{C_H^{*-1/\theta}}{C_F^{*-1/\theta}} = \frac{P_H^*}{P_F^*}.$$

Then,

$$\frac{C_H}{C_F} = p^\theta, \quad \frac{C_H^*}{C_F^*} = (p^*)^\theta \quad (2)$$

Combining equations (1) and (2) implies

$$\frac{C_H}{C_F} = (1 - \tau)^{-2\theta} \frac{C_H^*}{C_F^*}. \quad (3)$$

# Home bias in trade

Consider the symmetric case where  $Y_H = Y_F$ . Then,  $\frac{C_H}{C_F} = \frac{C_F^*}{C_H^*}$ .

Then equation (3) reduces to

$$\frac{C_H}{C_F} = \frac{C_F^*}{C_H^*} = (1 - \tau)^{-\theta} = p^\theta.$$

Then

$$\frac{P_H C_H}{P_F C_F} = \frac{C_H}{p C_F} = p^{\theta-1} = (1 - \tau)^{1-\theta}$$

and

$$\frac{P_F^* C_F^*}{P_H^* C_H^*} = \frac{p^* C_F^*}{C_H^*} = p^\theta p^* = p^{\theta+1} (1 - \tau)^2 = (1 - \tau)^{1-\theta}.$$



# Home bias in trade - numerical results

- If  $\tau = 0$ , then  $\frac{C_H}{pC_F} = 1$ .
- If  $\tau = 0.25$  and  $\theta = 6$ , then  $\frac{C_H}{pC_F} = 4.2$ .

# Home bias in trade - preferences

Now consider home bias  $\omega < 1$  in preferences

$$U \equiv \left( C_H^{(\theta-1)/\theta} + \omega C_F^{(\theta-1)/\theta} \right)^{\theta/(\theta-1)}$$

and

$$U \equiv \left( \omega C_H^{*(\theta-1)/\theta} + C_F^{*(\theta-1)/\theta} \right)^{\theta/(\theta-1)}$$

## Example

Show that the effects of home bias in preferences ( $\omega < 1$ ) can be isomorphic to the effects of trade costs  $\tau$ .

## Puzzle 2: Feldstein-Horoika puzzle

- Theory:
  - savings flow to countries with the most productive investment opportunities
  - domestic saving rates would be uncorrelated with domestic investment rates
- Feldstein and Horoika (1980) documented that national savings rates are highly correlated with domestic investment rates (long period averages)

# Puzzle 2: Feldstein-Horoika puzzle

- Feldstein and Horioka regressions:

Feldstein-Horioka Regressions, 1990–1997<sup>a</sup>

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$$\frac{I}{Y} = \alpha + \beta \frac{NS}{Y} + \epsilon$$

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	No. of Observ.	$\alpha$	$\beta$	R <sup>2</sup>
All countries <sup>b</sup>	56	0.15 (0.02)	0.41 (0.08)	0.33
Countries with GNP/cap > 1000	48	0.13 (0.02)	0.48 (0.09)	0.39
Countries with GNP/cap > 2000	41	0.07 (0.02)	0.70 (0.09)	0.62
OECD countries <sup>c</sup>	24	0.08 (0.02)	0.60 (0.09)	0.68

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<sup>a</sup>OLS regressions. Standard errors in parentheses.

# Feldstein-Horoika puzzle - a model

Consider a two-period, two-good, small-country endowment model.  
The utility function of a representative home resident is

$$u(C_1) + \delta u(C_2)$$

where

$$C \equiv \left( C_H^{(\theta-1)/\theta} + C_F^{(\theta-1)/\theta} \right)^{\theta/(\theta-1)} .$$

# Feldstein-Horoika puzzle - budget constraints

The small country is endowed with  $Y_{H,1}$  in period 1, and  $Y_{H,2}$  in period 2. It takes as given world prices  $P_H^*$ ,  $P_F^*$ ,  $r^*$ . The first and second period budget constraints are given by

$$P_{H,1}C_{H,1} + P_{F,1}C_{F,1} \leq P_{H,1}Y_{H,1} + D$$

$$P_{H,2}C_{H,2} + P_{F,2}C_{F,2} \leq P_{H,2}Y_{H,2} - (1 + r^*) D$$

# Feldstein-Horoika puzzle - first order conditions

FOCs are given by

$$(C_{H,1})^{-1/\theta} C^{1/\theta} = P_{H,1} \lambda_1 \quad (4)$$

$$(C_{F,1})^{-1/\theta} C^{1/\theta} = P_{F,1} \lambda_1 \quad (5)$$

# Feldstein-Horoika puzzle

Combine equations (4) and (5),

$$\begin{aligned} \left( C_{H,1}^{(\theta-1)/\theta} + C_{F,1}^{(\theta-1)/\theta} \right) C^{(1-\theta)/\theta} &= (P_{H,1}^{1-\theta} + P_{F,1}^{1-\theta}) \lambda_1^{1-\theta} \\ \left( C_{H,1}^{(\theta-1)/\theta} + C_{F,1}^{(\theta-1)/\theta} \right)^{\theta/(\theta-1)} C^{-1} &= (P_{H,1}^{1-\theta} + P_{F,1}^{1-\theta})^{\theta/(\theta-1)} \lambda_1^{-\theta} \\ \lambda_1 &= P_1^{-1} \end{aligned}$$

where

$$P_1 = (P_{H,1}^{1-\theta} + P_{F,1}^{1-\theta})^{1/(1-\theta)} \quad (6)$$



# Feldstein-Horoika puzzle

Therefore the consumption of home and foreign goods are

$$C_{H,t} = \left( \frac{P_{H,t}}{P_t} \right)^{-\theta} C_t, \quad C_{F,t} = \left( \frac{P_{F,t}}{P_t} \right)^{-\theta} C_t \quad t = 1, 2 \quad (7)$$

The first period budget constraint can be written as

$$\begin{aligned} P_{H,1} C_{H,1} + P_{F,1} C_{F,1} &= P_{H,1}^{1-\theta} P_1^\theta C_1 + P_{F,1}^{1-\theta} P_1^\theta C_1 \\ &= (P_{H,1}^{1-\theta} + P_{F,1}^{1-\theta}) P_1^\theta C_1 \\ &= P_1 C_1 \\ &\leq P_{H,1} Y_{H,1} + D \end{aligned}$$

# Feldstein-Horoika puzzle

Similarly, the second period budget constraint is

$$P_2 C_2 \leq P_{H,2} Y_{H,2} - (1 + r^*)D$$

Combining the budget constraints,

$$P_1 C_1 + \frac{P_2 C_2}{1 + r^*} = P_{H,1} Y_{H,1} + \frac{P_{H,2} Y_{H,2}}{1 + r^*}.$$

# Feldstein-Horoika puzzle

Let the domestic real interest rate be defined as

$$1 + r = (1 + r^*)P_1/P_2, \quad (8)$$

Then the consolidated intertemporal budget constraint is

$$C_1 + \frac{C_2}{1 + r} = \frac{P_{H,1}}{P_1} Y_{H,1} + \frac{P_{H,2}}{P_2} \frac{Y_{H,2}}{1 + r}.$$

Given  $P_1$  and  $P_2$ , equation (8) determines the real interest rate faced by domestic agent.

## Import home good in period 2

If the home good must be imported in period 2, while exported in period 1,  $P_{H,1} = P_H^*(1 - \tau)$  and  $P_{H,2} = P_H^*/(1 - \tau)$ . The domestic real interest rate is then given by

$$\begin{aligned} 1 + r &= (1 + r^*)P_1/P_2 \\ &= \frac{(1 + r^*) \left( (P_H^*(1 - \tau))^{1-\theta} + P_F^{1-\theta} \right)^{1/(1-\theta)}}{\left( (P_H^*/(1 - \tau))^{1-\theta} + P_F^{1-\theta} \right)^{1/(1-\theta)}} \\ &< 1 + r^* \end{aligned}$$

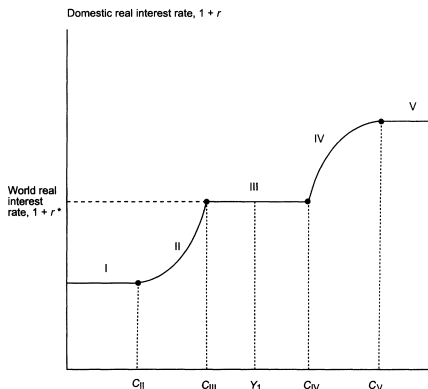
## Export home good in period 2

If the home good is exported in period 2, while imported in period 1,  $P_{H,1} = P_H^*/(1 - \tau)$  and  $P_{H,2} = P_H^*(1 - \tau)$ . The domestic real interest rate is then given by

$$\begin{aligned} 1 + r &= (1 + r^*)P_1/P_2 \\ &= \frac{(1 + r^*) \left( (P_H^*/(1 - \tau))^{1-\theta} + P_F^{1-\theta} \right)^{1/(1-\theta)}}{\left( (P_H^*(1 - \tau))^{1-\theta} + P_F^{1-\theta} \right)^{1/(1-\theta)}} \\ &> 1 + r^* \end{aligned}$$

# Small current account balance

If the country runs a sufficiently small current account balance, then there is never a reversal in trade patterns. In this region,  $1 + r = 1 + r^*$ , and trade costs have no effect on the domestic real interest rate.

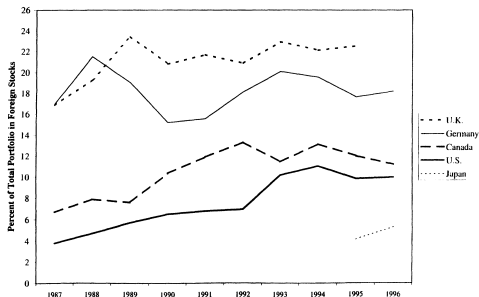


# Numerical Example

- If  $r^* = 0.05$ ,  $\tau = 0.1$ ,  $\theta = 0.6$ ,  $P_H^* = P_F^* = 1$ , the highest possible real interest rate is 20 percent, while the lowest is -8 percent
- This can put a check on a country's incentives to run large current account deficits or surpluses (and thus large savings-investment differentials)

# Puzzle 3: Home bias in equity portfolios

- Americans and Japanese held 94 and 98 percent of their equity wealth in their respective domestic stock markets (French and Poterba 1991)
- By mid 90s, 10 percent of American equity was invested abroad (Tesar and Werner 1998)



From Tesar and Werner (1998)



# Arrow-Debreu Allocation

- Two-country, general equilibrium model
- Each country has a random endowment of its distinct perishable consumption good
- Countries are symmetric, and national endowments  $s = (Y_H, Y_F)$  follow a symmetric joint distribution
- Free and costless trade in Arrow-Debreu securities
- Agents choose state-contingent consumptions  $C_H$  and  $C_F$  of the home and foreign goods to maximize

$$EU = E \left\{ \frac{1}{1-\rho} \left[ \left( C_H^{(\theta-1)/\theta} + C_F^{(\theta-1)/\theta} \right)^{\theta/(\theta-1)} \right]^{1-\rho} \right\} = E \frac{C^{1-\rho}}{1-\rho}.$$

# First Order Conditions

FOCs are given by

$$\frac{P_F(s)}{P_H(s)} C_H(s)^{-1/\theta} = C_F(s)^{-1/\theta}$$

$$\frac{P_F^*(s)}{P_H^*(s)} (C_H^*(s))^{-1/\theta} = (C_F^*(s))^{-1/\theta}$$

$$C_H(s)^{-1/\theta} C(s)^{1/\theta-\rho} = (1-\tau) C_H^*(s)^{-1/\theta} C^*(s)^{1/\theta-\rho} \quad (9)$$

$$(1-\tau) C_F(s)^{-1/\theta} C(s)^{1/\theta-\rho} = C_F^*(s)^{-1/\theta} C^*(s)^{1/\theta-\rho} \quad (10)$$

Together, these conditions imply ex post consumption efficiency

$$\left( \frac{P_F(s)}{P_H(s)} \right)^\theta = \frac{C_H(s)}{C_F(s)} = (1-\tau)^{-2\theta} \frac{C_H^*(s)}{C_F^*(s)} = (1-\tau)^{-2\theta} \left( \frac{P_F^*(s)}{P_H^*(s)} \right)^\theta$$

# Arrow-Debreu Allocation

The model is closed by the output-market clearing conditions:

$$C_H^*(s) = (1 - \tau)(Y_H(s) - C_H(s)) \quad (11)$$

$$C_F(s) = (1 - \tau)(Y_F(s) - C_F^*(s)) \quad (12)$$

We have four equations, (9)-(12), and four unknowns,

$C_H, C_F, C_H^*, C_F^*$  for every state  $s$ .

# Arrow-Debreu Allocation

Assume that  $\rho = 1/\theta$ . Then

$$C_H(s) = \frac{1}{1 + (1 - \tau)^{\theta-1}} Y_H(s)$$

$$C_F(s) = \frac{(1 - \tau)^\theta}{1 + (1 - \tau)^{\theta-1}} Y_F(s)$$

Equity shares are given by

$$X_H = \frac{1}{1 + (1 - \tau)^{\theta-1}} Y_H$$

$$X_F = \frac{(1 - \tau)^{\theta-1}}{1 + (1 - \tau)^{\theta-1}} Y_F$$

# Arrow-Debreu Allocation

In the absence of trade costs, equity shares are  $1/2$ .

For  $\theta = 6$  and  $\tau = 0.25$ , then  $X_H = 0.81$

# Equity Trade Allocation

Now consider the model without Arrow-Debreu securities, but with trade in equity shares to each country's output.

## Example

Assume that  $\rho = 1/\theta$ . Show that the equity trade allocation is identical to the Arrow-Debreu allocation.

## Puzzle 4: Consumption correlations puzzle

- Consider a one-good, two-country model with free trade and complete markets in which all agents have an identical period utility function:

$$u(C) = \frac{C^{1-\rho}}{1-\rho}$$

- Then home and foreign consumption growth rates are equalized:

$$\frac{C_{t+1}}{C_t} = \frac{C_{t+1}^*}{C_t^*}$$

- Empirically, consumption growth rates are much less correlated

## Puzzle 5: Purchasing-power-parity puzzle

- Let  $Q$  be the real exchange rate between two countries

$$Q = e \frac{P^*}{P}$$

where  $e$  is the nominal exchange rate

- Consider the regression:

$$\log Q_t = \alpha + \eta t + \gamma \log Q_{t-1} + \epsilon_t$$

- $\gamma$  ranges from 0.99 (US-Canada; half-life of 69 months) to 0.97 (Germany-Japan; 21 months)
- Half-lives of this magnitude are hard to understand if financial-market disturbances with only transitory real effects are very important in explaining short-run volatility.



## Puzzle 6: Exchange rate disconnect puzzle

- Remarkably weak short-term feedback links between exchange rate and the rest of the economy
- PPP puzzle is a special case
- Similar to stock-price disconnect puzzle, but links between exchange rate and real economy are much more direct than for stock prices
- A model with imperfect markets, trade costs, and nominal rigidities can produce a disconnect in which the exchange rate responds wildly to shocks