

# Lecture 10: Chapter 5, Section 2

## Relationships (Two Categorical Variables)

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- Two-Way Tables
- Summarizing and Displaying
- Comparing Proportions or Counts
- Confounding Variables

# Looking Back: *Review*

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## □ 4 Stages of Statistics

- Data Production (discussed in Lectures 1-4)
- Displaying and Summarizing
  - Single variables: 1 cat, 1 quan (discussed Lectures 5-8)
  - Relationships between 2 variables:
    - Categorical and quantitative (discussed in Lecture 9)
    - Two categorical
    - Two quantitative
- Probability
- Statistical Inference



# Single Categorical Variables (*Review*)

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## □ **Display:**

- Pie Chart

- Bar Graph

## □ **Summarize:**

- Count or Proportion or Percentage

Add categorical explanatory variable →  
display and summary of categorical responses  
are **extensions** of those used for single  
categorical variables.

## Example: *Two Single Categorical Variables*

- **Background:** Data on students' gender and lenswear (contacts, glasses, or none) in two-way table:

	Contacts	Glasses	None	Total
Female	121	32	129	282
Male	42	37	85	164
Total	163	69	214	446

- **Question:** What parts of the table convey info about the *individual variables* gender and lenswear?
- **Response:**
  - \_\_\_\_\_ is about gender.
  - \_\_\_\_\_ is about lenswear.

## Example: *Relationship between Categorical Variables*

- **Background:** Data on students' gender and lenswear (contacts, glasses, or none) in two-way table:

	Contacts	Glasses	None	Total
Female	121	32	129	282
Male	42	37	85	164
Total	163	69	214	446

- **Question:** What part of the table conveys info about the *relationship* between gender and lenswear?
- **Response:** \_\_\_\_\_ is about relationship.

# Summarizing and Displaying Categorical Relationships

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- Identify variables' **roles** (explanatory, response)
- Use **rows for explanatory**, columns for response
- **Compare proportions** or percentages in response of interest (*conditional proportions or percentages*) for various explanatory groups.
- Display with **bar graph**:
  - Explanatory groups identified on **horizontal** axis
  - Conditional percentages or proportions in response(s) of interest graphed **vertically**



# Definition

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- A **conditional** percentage or proportion tells the percentage or proportion in the response of interest, given that an individual falls in a particular explanatory group.

## Example: Comparing Counts vs. Proportions

- **Background:** Data on students' gender and lenswear (contacts, glasses, or none) in two-way table:

	Contacts	Glasses	None	Total
Female	121	32	129	282
Male	42	37	85	164
Total	163	69	214	446

- **Question:** Since 129 females and 85 males wore no lenses, should we report that fewer males wore no lenses?
- **Response:**
  - **proportion** of females with no lenswear:
  - **proportion** of males with no lenswear:

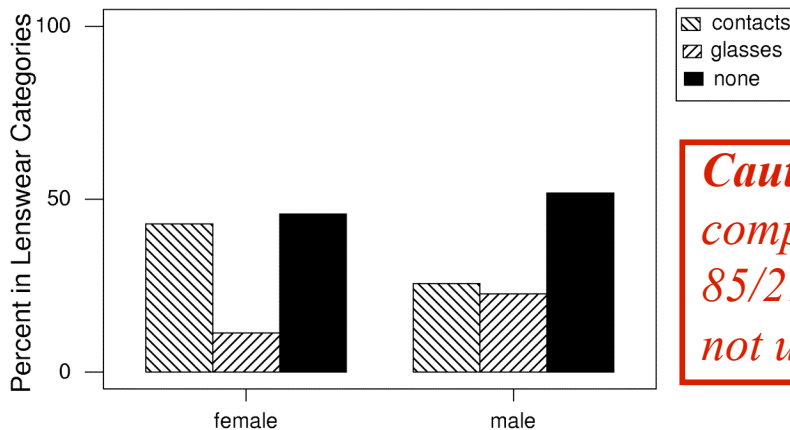


# Example: *Displaying Categorical Relationship*

- **Background:** Counts and conditional percentages produced with software:

Rows: Gender	Columns: Lenswear			
	contacts	glasses	none	All
female	121	32	129	282
	42.91	11.35	45.74	100.00
male	42	37	85	164
	25.61	22.56	51.83	100.00
All	163	69	214	446

- **Question:** How can we display this information?
- **Response:**



**Caution:** If we made lenswear explanatory, we'd compare  $129/214 = 60\%$  with no lenses female,  $85/214 = 40\%$  with no lenses male, etc. Why is this not useful?

# Example: *Interpreting Results*

- **Background:** Counts and conditional percentages produced with software:

Rows: Gender	Columns: Lenswear			
	contacts	glasses	none	All
female	121	32	129	282
	42.91	11.35	45.74	100.00
male	42	37	85	164
	25.61	22.56	51.83	100.00
All	163	69	214	446

- **Questions:** Are you convinced that, **in general**,
  - all females wear contacts more than males do?
  - all males are more likely to wear no lenses?
- **Responses:** Consider *how* different sample percentages are:
  - Contacts:
  - No lenses:

*Looking Ahead: Inference will let us judge if sample differences are large enough to suggest a general trend. For now, we can guess that the first difference is “real”, due to different priorities for importance of appearance.*

## Example: *Comparing Proportions*

- **Background:** An experiment considered if wasp larvae were less likely to attack an embryo if it was a brother:

	Attacked	Not attacked	Total
Brother	16	15	31
Unrelated	24	7	31
Total	40	22	62

- **Question:** What are the relevant proportions to compare?
- **Response:**
  - Brother: \_\_\_\_\_ were attacked
  - Unrelated: \_\_\_\_\_ were attacked
  - \_\_\_\_\_ likely to attack a brother wasp



## Another Comparison in Considering Categorical Relationships

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- Instead of considering how different are the *proportions* in a two-way table, we may consider how different the *counts* are from what we'd expect if the “explanatory” and “response” variables were in fact unrelated.

## Example: *Expected Counts*

- **Background:** Experiment considered if wasp larvae were less likely to attack embryo if it was a brother:

	Attacked	Not attacked	Total
Brother	16	15	31
Unrelated	24	7	31
Total	40	22	62

- **Question:** What counts would we **expect** to see, if being a brother had no effect on likelihood of attack?
- **Response:** Overall 40/62 attacked → expect \_\_\_\_\_ brothers, \_\_\_\_\_ unrelated to be attacked; expect remaining \_\_\_\_\_ brothers and \_\_\_\_\_ unrelated not to be attacked.

## Example: Comparing Counts

- **Background:** Tables of observed and expected counts in wasp aggression experiment:

Obs	A	NA	T
B	16	15	31
U	24	7	31
T	40	22	62

Exp	A	NA	T
B	20	11	31
U	20	11	31
T	40	22	62

- **Question:** How do the counts compare?
- **Response:**

*Looking Ahead: Inference (Part 4) will help decide if these differences are large enough to provide evidence that kinship and aggression are related.*

## Example: *Expected Counts in Lenswear Table*

- **Background:** Data on students' gender and lenswear (contacts, glasses, or none) in two-way table:

	C	G	N	Total
F	121	32	129	282
M	42	37	85	164
Total	163	69	214	446

- **Question:** What counts would we expect to wear glasses, if there were no relationship between gender and lenswear?
- **Response:** Altogether, 69/446 wore glasses. If there were no relationship, we'd expect \_\_\_\_\_ females and \_\_\_\_\_ males with glasses.

## Example: *Observed vs. Expected Counts*

- **Background:** If gender and lenswear were unrelated, we'd expect 44 females and 25 males with glasses.

	C	G	N	Total
F	121	32	129	282
M	42	37	85	164
Total	163	69	214	446

- **Question:** How different are the observed and expected counts of females and males with glasses?
- **Response:** Considerably \_\_\_\_\_ females and \_\_\_\_\_ males wore glasses, compared to what would be expected if there were no relationship.



# Confounding Variable in Categorical Relationships

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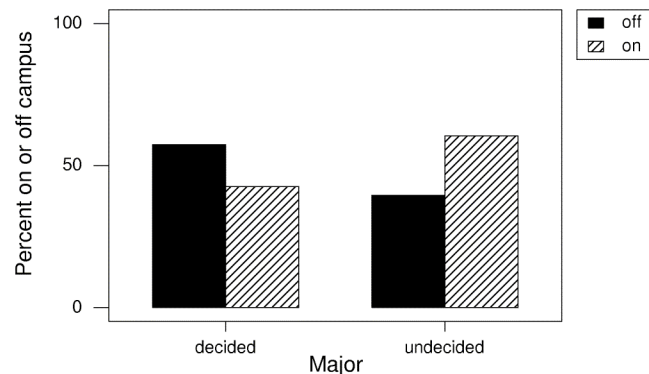
- If data in two-way table arise from an **observational study**, consider possibility of confounding variables.

***Looking Back:** Sampling and Design issues should always be considered before reporting summaries of single variables or relationships.*

## Example: *Confounding Variables*

- **Background:** Survey results for full-time students:

	On Campus	Off Campus	Total	Rate On Campus
Undecided	124	81	205	$124/205=60\%$
Decided	96	129	225	$96/225=43\%$

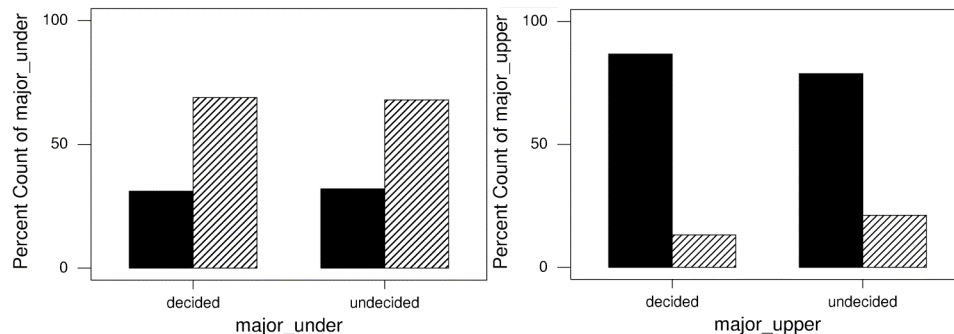


- **Question:** Is there a relationship between whether or not major is decided and living on or off campus?
- **Response:**


# Example: Handling Confounding Variables

- **Background:** Year at school may be confounding variable in relationship between major decided or not and living situation.
- **Question:** How should we handle the data?
- **Response:**

<b>Underclassmen</b>	On Campus	Off Campus	Total	Rate On Campus
Undecided	117	55	172	$117/172=68\%$
Decided	82	37	119	$82/119=69\%$
<b>Upperclassmen</b>	On Campus	Off Campus	Total	Rate On Campus
Undecided	7	26	33	$7/33=21\%$
Decided	14	92	106	$14/106=13\%$



**Underclassmen** (1st&2nd yr): proportions on campus are \_\_\_\_\_ for those with major decided or not. **Upperclassmen** (3rd & 4th yr): proportions are \_\_\_\_\_.



# Simpson's Paradox

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If the nature of a relationship changes, depending on whether groups are combined or kept separate, we call this phenomenon “Simpson's Paradox”.



## **Example:** *Considering Confounding Variables*

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- **Background:** Suppose that boys, like Bart, tend to eat a lot of sugar and they also tend to be hyperactive. Girls, like Lisa, tend not to eat much sugar and they are less likely to be hyperactive.
- **Question:** Why would the data lead to a misperception that sugar causes hyperactivity?
- **Response:**



# Lecture Summary

## *(Categorical Relationships)*

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- **Two-Way Tables**
  - Individual variables in margins
  - Relationship inside table
- **Summarize:** Compare (conditional) proportions.
- **Display:** Bar graph
- **Interpreting Results:** How different are proportions?
- **Comparing Observed and Expected Counts**
- **Confounding Variables**