

## Lecture 17

### Chapter 15 Understanding and Reporting Trends over Time; Review

- Time Series
- 4 Features of Time Series
- Review of Part Two

## Constructing & Summarizing a Time Series

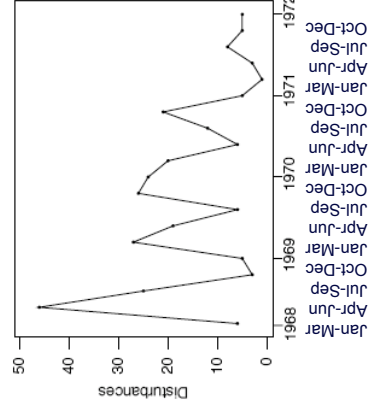
- Horizontal axis for time, vertical for responses
- Connect the dots
- Consider main features:
  - Long-term trend
  - Seasonal components
  - Irregular cycles
  - Random fluctuations

## Example: Visualizing a Time Series

- **Background:** Suppose you recorded the number of hours spent on homework each week over 4 years.
- **Question:** What would the time series plot show?
- **Response:**
  - Long-term trend:
  - Seasonal components:
  - Irregular cycles:
  - Random fluctuations:

## Example: Analyzing a Time Series

- **Background:** Civil disturbances in U.S., 1968-1970.

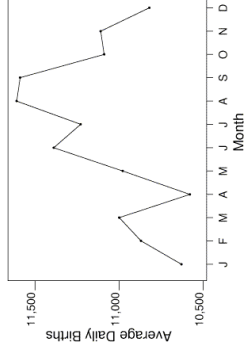


### Example: Analyzing a Time Series

- **Background:** Civil disturbances in U.S., 1968-1972:
- **Question:** What does the time series plot show?
- **Response:**
  - Long-term trend:
  - Seasonal components:
  - Irregular cycles:
  - Random fluctuations:

### Example: Time Series: Lows and Highs

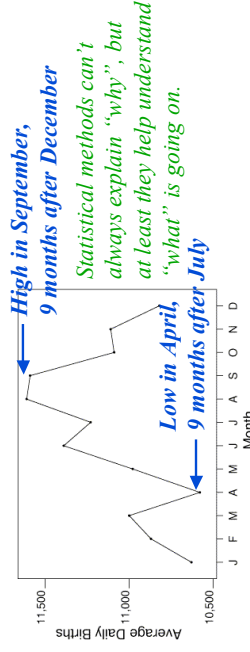
- **Background:** Time series plot shows average daily births each month in year 2000 in the U.S.:



- **Question:** Where do you see a low and a high?
- **Response:**

### Example: Time Series: Lows and Highs

- **Background:** Time series plot shows average daily births each month in year 2000 in the U.S.:



- **Questions:** How can we explain why there are...
  - Conceptions in U.S.: fewer in July, more in December?
  - Conceptions in Europe: more in summer, fewer in winter?
- **Response:**

### Significant Relation in 2 Cat. Vars. (Review)

1. Compute each expected count =  $\frac{\text{Column total} \times \text{Row total}}{\text{Table total}}$
2. Calculate each component =  $\frac{(\text{observed} - \text{expected})^2}{\text{expected}}$
3. Find chi-square = sum of  $\frac{(\text{observed} - \text{expected})^2}{\text{expected}}$
4. If chi-square > 3.84, there is a statistically significant relationship. Otherwise, we don't have evidence of a relationship.

### Example: Comparing Proportions

- **Background:** An experiment considered if wasp larvae were less likely to attack an embryo if it was a brother:

	Attacked	Not attacked	Total
Brother	16	15	31
Unrelated	24	7	31
Total	40	22	62

- **Question:** What are the relevant proportions to compare?
- **Response:**
  - Brother:
  - Unrelated:
  - → \_\_\_\_\_ likely to attack a brother wasp

### Example: Expected Counts

- **Background:** Kinship and aggression in wasps...

	Attacked	Not attacked	Total
Brother	16	15	31
Unrelated	24	7	31
Total	40	22	62

- **Question:** If kinship and aggression were not related, what counts would we expect?
- **Response:** Overall 40/62 attacked → expect \_\_\_\_\_ brothers, \_\_\_\_\_ unrelated to be attacked, remaining \_\_\_\_\_ brothers unattacked, \_\_\_\_\_ unrelated unattacked

### Example: Comparing Counts

- **Background:** Tables of observed and expected counts in wasp aggression experiment:

Obs	A	NA	T
B	16	15	31
U	24	7	31
T	40	22	62

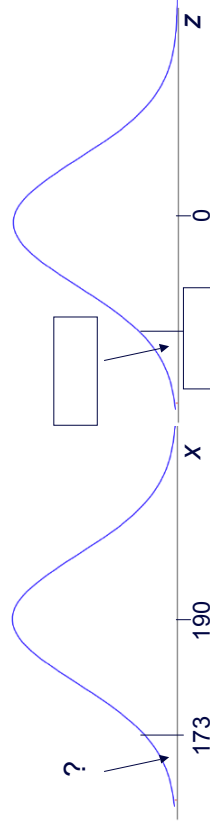
Exp	A	NA	T
B	20	11	31
U	20	11	31
T	40	22	62

- **Question:** What is chi-square? Conclude?
- **Response:**

Conclude kinship and aggression \_\_\_\_\_

### Example: Normal Exercise #1

- **Background:** Healthy cholesterol levels  $x$  are normal with mean 190, sd 10.
- **Question:** What % are below 173?
- **Response:**



### Example: Normal Exercises #2

- **Background:** Healthy cholesterol levels  $x$  are normal with mean 190, sd 10.
- **Questions:** What % are (a)  $> 182$  (b)  $< 234$  (c)  $> 192$
- **Responses:**

### Example: Normal Exercises #3

- **Background:**  $x$  is normal with mean 190, sd 10.
- **Questions:** (a) The lowest 5% are below what level?  
(b) The top 20% are above what level?
- **Responses:**

### Example: Smoking and Alcohol Related?

- **Background:** Overall proportion alcoholic is  $\frac{40}{1000} = 0.04$

Obs	D	ND	T
V	14	18	32
P	15	7	22
T	29	25	54

- **Questions:** What counts do we expect if no relationship?
- **Response:** Expect...
  - \_\_\_\_\_ smokers to be alcoholic
  - \_\_\_\_\_ non-smokers to be alcoholic
  - \_\_\_\_\_ smokers not alcoholic
  - \_\_\_\_\_ non-smokers not alcoholic

### Example: Smoking & Alcohol (continued)

- **Background:** Observed and Expected Tables:

Obs	A	NA	Total	Exp	A	NA	Total
S	30	200	230	S	9.2	220.8	230
NS	10	760	770	NS	30.8	739.2	770
Total	40	960	1000	Total	40	960	1000

- **Question:** Find components & chi-square; conclude?
- **Response:** chi-square

The relationship is significant, because