

Chem 2430 - HW #1

Assigned 9/1/2021, Due 9/9/2021

1. Assume that the wavefunction of a system is  $\psi = e^{-ax^2} + xe^{-ax^2}$  and that  $x$  extends from  $-\infty$  to  $\infty$ 
  - a) What is the normalized wavefunction?
  - b) What is the probability of finding the particle between  $x = -1$  and  $x = +1$ ?
  - c) Are  $e^{-ax^2}$  and  $xe^{-ax^2}$  orthogonal on  $(-\infty, \infty)$ ? on  $(0, \infty)$ ?
2. Consider the wave function  $\psi = Ae^{ikx} + Be^{-ikx}$  for the system with  $V = \infty, x \leq a$  and  $V = 0, x > a$ .
  - a) Determine  $A$  and  $B$ .
  - b) Derive the energy of this system.
3. What is the zero-point energy of an electron in a 1D box of length 10 Bohr's? Give your result in electronvolts.