

CHEM 2430 HW #8

1. Explain why $e^{-cr_1} e^{-cr_2} (r_1 - r_2)$ is not a suitable trial function for the He atom?

2. Write a proper wavefunction for the ground state of positronium (e^+ , e^-) including spin.

3. Show that $\hat{S}_z = \frac{1}{2}\hbar \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$, $\hat{S}_y = \frac{1}{2}\hbar \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$, $\hat{S}^2 = \frac{1}{4}\hbar^2 \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$ in a matrix representation.

4. For an atom with a $\dots d^2$ configuration (where \dots denotes a closed shell), what electronic states can result, indicating both angular momentum and spin?

What state do you expect to be in lowest energy?

5. The $2s \rightarrow 2p$ excited states of the Be atom are relatively low-lying in energy. In light of that, write down a wavefunction for the ground state that includes s/p mixing.