

**Due January 28, 1999**

1. Confirm that  $\psi = xe^{-ax^2}$  is a solution of the Schrödinger Equation for the harmonic oscillator and find  $a$ .
2. Calculate  $\langle x^2 \rangle$  for the ground state of a harmonic oscillator. (See Table 12.1)
3. Show that for a harmonic oscillator the selection rule for IR transitions is  $\Delta V = \pm 1$ .
4. Consider the particle-on-a-ring problem. What is the  $z$ -component of the angular momentum if  $\psi = e^{3i\phi}$ , if  $\psi = ae^{i\phi} + be^{-i\phi}$ ?
5. Problem 12.21 from text.
6. Consider the H atom. Is the electron further from the nucleus on average when it is in a 2p or 2s orbital?
7. Show that  $\hat{l}^2$  and  $\hat{l}_z$  commute with one another. Show also that they commute with  $\hat{H}$  for the H atom. Why is this important?