

SOLUTION MANUAL FOR HW # 5

7.17)

${}^1\text{H}{}^{19}\text{F}$

$$E_l = \frac{\hbar^2}{2I} l(l+1) \quad \& \quad I = \mu r^2$$

$$m_H = 1.008 * 1.67 * 10^{-27} \text{ kg} = 1.68 * 10^{-27} \text{ kg}$$

$$m_{Cl} = 34.98 * 1.67 * 10^{-27} \text{ kg} = 58.42 * 10^{-27} \text{ kg}$$

$$\mu = \frac{m_H m_{Cl}}{m_H + m_{Cl}} = 1.586 * 10^{-27} \text{ kg} \Rightarrow I = 1.33 * 10^{-47} \text{ kgm}^2$$

$$E_l = 4.16 * 10^{-22} l(l+1) J$$

a) $E_0 = 0 J$

b) $E_1 = 8.33 * 10^{-22} J \Rightarrow \Delta E_{0 \rightarrow 1} = 8.33 * 10^{-22} J$

7.20)

$$E_J = BJ(J+1) \quad \& \quad \frac{n_J}{n_0} = \frac{g_J}{g_0} e^{-\Delta E_{J-0}/kT} \quad \& \quad B = \frac{\hbar^2}{2I} \quad \& \quad g_J = 2J+1$$

$$I = 2.644 * 10^{-47} \text{ kgm}^2 \Rightarrow B = 2.10 * 10^{-22} J \quad \& \quad T = 298 K \Rightarrow kT = 4.13 * 10^{-21} J$$

$$E_0 = 0 \Rightarrow \Delta E_{J-0} = E_J = BJ(J+1) \Rightarrow \therefore \frac{\Delta E_{J-0}}{kT} = \frac{B}{kT} J(J+1) = 0.05085 J(J+1)$$

$$\frac{n_J}{n_0} = (2J+1) e^{-\Delta E_{J-0}/kT} = (2J+1) e^{-0.05085 J(J+1)}$$

$$J = 0 \Rightarrow \frac{n_J}{n_0} = 1$$

$$J = 5 \Rightarrow \frac{n_J}{n_0} = (2 * 5 + 1) e^{-0.05085 * 5(5+1)} = 2.38$$

$$J = 10 \Rightarrow \frac{n_J}{n_0} = (2 * 10 + 1) e^{-0.05085 * 10(10+1)} = 0.077$$

$$J = 20 \Rightarrow \frac{n_J}{n_0} = (2 * 20 + 1) e^{-0.05085 * 20(20+1)} = 2.08 * 10^{-8}$$

7.24)

a)

$$\mu = \left(\frac{1 \cdot 35}{1 + 35}\right) * 1.066 * 10^{-27} \text{ kg} = 1.61 * 10^{-27} \text{ kg}$$

$$E_{\text{Vibrational}} = \hbar \sqrt{\frac{k}{\mu}} = (1.055 * 10^{-34} \text{ J}) \sqrt{\frac{516 \text{ Nm}^{-1}}{1.61 * 10^{-27} \text{ kg}}} = 2.98 * 10^{-20} \text{ J}$$

$$I = \mu r^2 = 2.60 * 10^{-47} \text{ kgm}^2$$

$$E_{10} = \frac{\hbar^2}{2I} = 2.14 * 10^{-22} * 10 * (10 + 1) = 2.55 * 10^{-20} \text{ J}$$

$$kT = 4.14 * 10^{-21} \text{ J} \Rightarrow \frac{E_V}{kT} = 7.20 \quad \& \quad \frac{E_{10}}{kT} = 6.16$$

b)

$$\nu_V = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} = 0.88 * 10^{14} \text{ s}^{-1} \Rightarrow \tau = 1.125 * 10^{-14} \text{ s}$$

$$\nu_r = \frac{E_r}{h} = 3.85 * 10^{13} \text{ s}^{-1} \Rightarrow \tau = 2.59 * 10^{-14} \text{ s}$$

7.26)

$$p_x = \sqrt{\frac{3}{4\pi}} \sin \theta \cos \varphi \quad \& \quad d_{xz} = \sqrt{\frac{15}{4\pi}} \sin \theta \cos \theta \cos \varphi \quad \& \quad \hat{l}_z = -i\hbar \frac{\partial}{\partial \varphi}$$

$$\hat{l}_z p_x = -i\hbar \frac{\partial}{\partial \varphi} \left(\sqrt{\frac{3}{4\pi}} \sin \theta \cos \varphi \right) = i\hbar \sqrt{\frac{3}{4\pi}} \sin \theta \sin \varphi \Rightarrow NO$$

$$\hat{l}_z d_{xz} = -i\hbar \frac{\partial}{\partial \varphi} \left(\sqrt{\frac{15}{4\pi}} \sin \theta \cos \theta \cos \varphi \right) = i\hbar \sqrt{\frac{15}{4\pi}} \sin \theta \cos \theta \sin \varphi \Rightarrow NO$$