

1. Complete these problems from the book:

(a) p.103, Exercise 3.1.9

(b) p.108, Exercise 3.2.1

(c) p.109, Exercise 3.2.3, Exercise 3.2.4, Exercise 3.2.5, Exercise 3.2.9, Exercise 3.2.11

2. Show that any continuous map $f : \mathbb{R} \rightarrow \mathbb{Z}$ is constant.

3. Recall the notion of open sets $A \subset \mathbb{R}$.

$$A \subset \mathbb{R} \text{ is open} \Leftrightarrow \forall x_0 \in A : \exists \varepsilon > 0 : (x_0 - \varepsilon, x_0 + \varepsilon) \subset A.$$

Show the following. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a function. Then the following are equivalent

(a) $f : \mathbb{R} \rightarrow \mathbb{R}$ is continuous.

(b) the inverse f^{-1} maps open sets into open sets. That is: whenever $A \subset \mathbb{R}$ is an open set, then the $f^{-1}(A)$ defined as

$$f^{-1}(A) \equiv \{x \in \mathbb{R} : f(x) \in A\}$$

is an open set.